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QUICK ESTIMATES OF PEAK OVERPRESSURE FROM TWO SIMULTANEOUS BLAST WAVES

R & D Associates

P. O. Box 9695

Marina del Rey, California 90291

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December 1977

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SECTION 1. INTRODUCTION

Strong shocks in air reflect off rigid surfaces at many times (5-13 times) their original pressure. Opposing shocks of equal strength behave just as a reflected shock, leading to very high pressures at the initial point of contact. If two shocks of 100 psi collide, the resulting peak pressure is around 500. For two 1000-psi shocks, the peak pressure jumps to 8500 psi. This suggests that the area covered by a given overpressure from two simultaneous blast waves may be considerably large: than twice the area of a single burst.

Yet, while strong shock reflection factors are impressive, there is reason to believe that such high values do not extend far beyond the initial point of contact, and, further, two unequal shocks may interact in a much less impressive way. Strong blast waves are extremely transitory, and pressures, densities, and flow rates behind each blast front drop off exceedingly rapidly.

Careful considerations of such blast wave interactions lead directly to three-dimensional geometries which very much inhibit the accuracy and practical resolution achievable with canonical numerical methods. The following series of estimates, without benefit of rigorous modeling and detailed numerical calculations, are intended to bound the expectations for enhanced coverage by means of simultaneous blasts. Comparison is also made with the LAMB procedure, as applied to two simultaneous bursts and the overpressures along the line joining their centers.

^{*} Low-Altitude Multiple Burst.

SECTION 2. SEVERAL ESTIMATES

The peak overpressure from a single burst on the surface is well approximated with the formula [1]

$$\Delta P = \frac{3300 \text{ W}}{R^3} + \frac{192 \sqrt{W}}{R^{3/2}} \text{ psi}$$
 (1)

with W the yield in megatons and R the distance in kilofeet.

A normally reflected shock reaches a reflected pressure enhanced by the stagnation of the flow, and results in pressures for a strong shock much more than double the incident shock pressure. An approximate shock reflection factor for an ideal gas of specific heat ratio γ is given by

$$\frac{\Delta P_r}{\Delta P} = R = \frac{4\gamma P_o + (3\gamma - 1)\Delta P}{2\gamma P_o + (\gamma - 1)\Delta P}$$
 (2)

where ΔP is the incident overpressure, ΔP_{x} is the reflected overpressure, and P_{o} is the ambient pressure (14.7 psi). For sea level air, 1.1 < γ < 1.7 (γ = 1.3 for ΔP = 1000 psi)[1].

A more exact fit (within 3 percent) to this reflection factor is provided by the formula below, which accounts for the nonideal gas properties of sea level air [2].

^{*}This formula agrees to within 10 percent with the accepted average of the nuclear test data which in turn are 90 percent contained by a spread of ±50 percent at pressures above 40 psi.

$$RF = \frac{0.002655\Delta P}{1 + 0.0001728\Delta P + 1.921 \times 10^{-9} \Delta P^2} + 2$$

$$+ \frac{0.004218 + 0.04834\Delta P + 6.856 \times 10^{-6} \Delta P^{2}}{1 + 0.007997\Delta P + 3.844 \times 10^{-6} \Delta P^{2}} . (3)$$

At the point where two simultaneous spherical blast waves meet, the peak overpressure can be fairly precisely described with these two approximations (Equations 1 and 3). For example (as in Figure 1), for two 1-MT simultaneous surface explosions separated by 6860 ft, the blast waves meet when each has a peak overpressure of 116 psi (Equation 1), and these shocks reflect at the point of contact to a pressure of 600 psi (a reflection factor of 5.18) (Equation 3). The value of 600 psi from a single 1-MT surface burst occurs at 1840 ft. For nonsimultaneous bursts, a separation of 3680 ft would cover a line target with more than 600 psi everywhere. The separation distance at which the interacting shocks reflect to 600 psi (6660 ft) is nearly twice as long.

The area associated with the region of enhanced blast pressures is a thin lens about the point of contact between spherical (or hemispherical) shocks, and is only a small fraction of the area covered by the individual blast wares.

However, the use of the larger distance (6860 ft), where the shocks reflect to just 600 psi as an effective kill distance for a line target, is quite incorrect. The geometry of the situation (Figure 2) suggests that as the two shocks pass

It is very wrong to assume that if the separation distance were increased by a factor of two, the area coverage would be correspondingly increased by a factor of four.

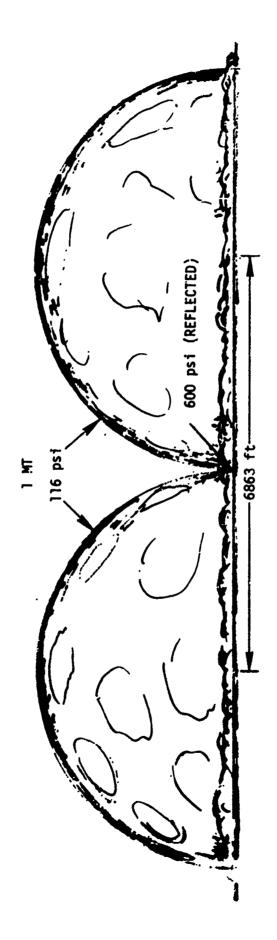


Figure 1. Two 1 MT Surface Bursts (Simultaneous) Reflecting to 600 psi

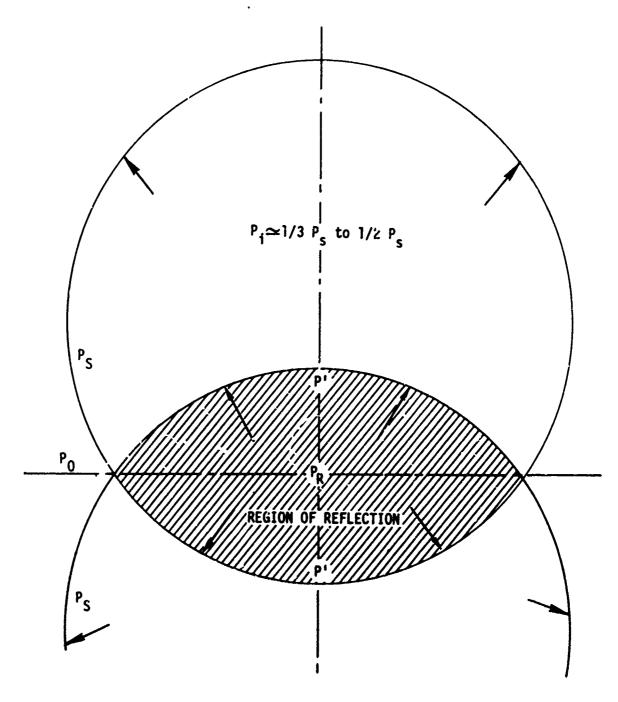


Figure 2. Geometry for Two Simultaneous Blast Waves Interacting

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through each other, they continue to expand spherically, and so drop rapid, in pressure from that peak value of first contact (Figure 1). If their peak interaction gives only 600 psi, then all the region between burst points that lies beyond a radius from each burst point of 1840 ft would see less than 600 tell (Figure 3). That is, as in Figure 3, a total of 3200 ft would experience two shocks—both less than 600 psi.

Of greater interest is the separation distance that exposes the entire line target to more than 600 psi (or some other peak overpressure of interest). For this we need to know how rapidly these diverging shocks decrease in overpressure as they expand into each other. Since, on first contact with the opposing blast waves the transmitted shock starts at the peak reflection value, the initial value is well defined (Equation 3), but there does not exist an equally simple or direct formula for predicting the subsequent decay rate as the two blasts penetrate each other.

Numerical blast calculations provide detailed descriptions of the pressure field into which each transmitted shock is expanding and how it behaves in both space and time [3,4,5]. For most applications to hard targets (e.g., for 600-psi trenches), a simple strong shock model would suffice. In any case, while peak pressure decays with distance (as in Equation 1) approximately in proportion to the inverse cube of the distance, the interior of the fireball/blast-wave follows with a pressure about one-third to one-half of the shock value (Figure 4). In fact, both peak pressure and interior pressure decrease in proportion to the inverse of the time measured from the instant of explosion. An approximate relation is given by [2]*

Two simpler but less exact forms for the pressure-time relation in a nuclear blast wave may be found in Reference 1, pp. 180-181.

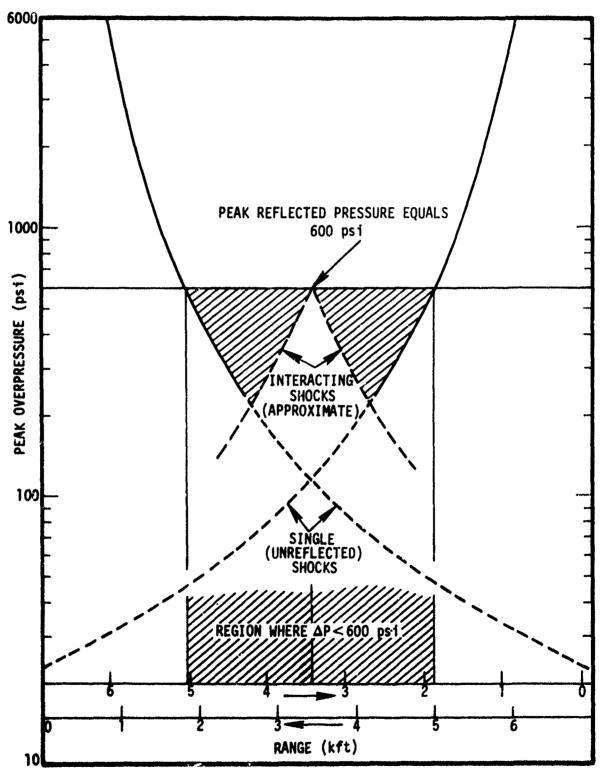
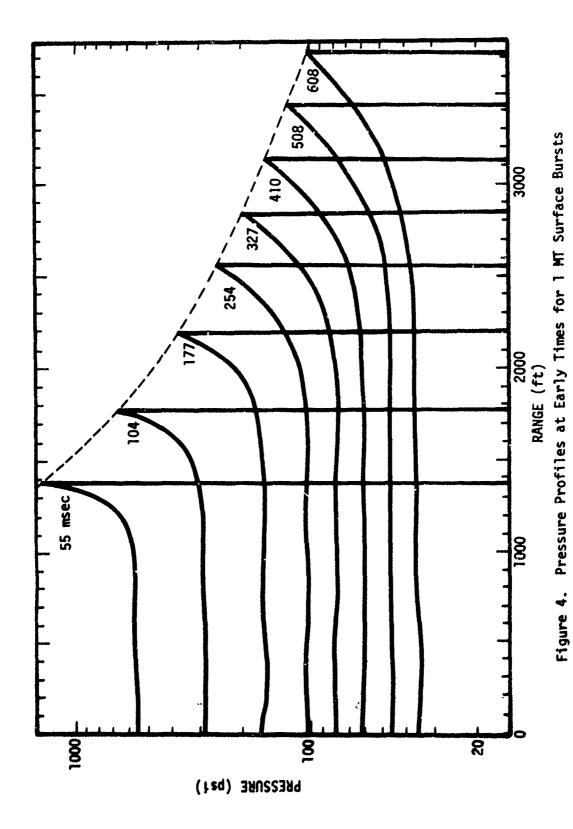


Figure 3. Peak Overpressure vs Range for Two 1 MT Simultaneous Surface Bursts Separated by 6860 ft



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$$\Delta P(t,T) \simeq \left(\frac{148000}{0.135 + t}\right) \left[0.417 + 0.583 \left(\frac{T}{t}\right)^{6}\right] \left(1 - \frac{t-T}{D}\right) f(t)$$
 (4)

in which t is the time in msec (after burst), T is the shock arrival time (msec) for 1 MT, ($t \ge T$), D is the positive phase duration (msec) (the time during which the blast pressure is greater than ambient), and f(t) is an empirical adjustment fit of secondary importance.

$$f(t) = \frac{100 + 6.72t + 0.00581t^2}{100 + 18.8t + 0.0216t^2} .$$
 (5)

The essential time behavior of the pressure is illustrated by this approximation: The dominant behavior is a decay almost linear in time (more precisely as $^{\circ}$ t^{-1.15}) with a very sharp drop just behind the shock front to a value of about 40 percent of that at the front ($^{\circ}$ t⁻⁶).

One possible approximation is to assume that the transmitted shock continues to generate the same peak reflection factor as it continues to expand and decrease inside the other blast wave. This is likely a gross overestimate of the off-peak pressures, since one might better use reflection factors appropriate to the transmitted shock as it continues to expand and decrease. The original blast that it is running into also continues to expand and decrease in pressure. A more correct approximation will account for this double decay, but, for the moment, consider several simple approximations for the transmitted peak over-pressure.

Figure 5 shows several choices for these transmitted pressures in the particular case of two simultaneous surface

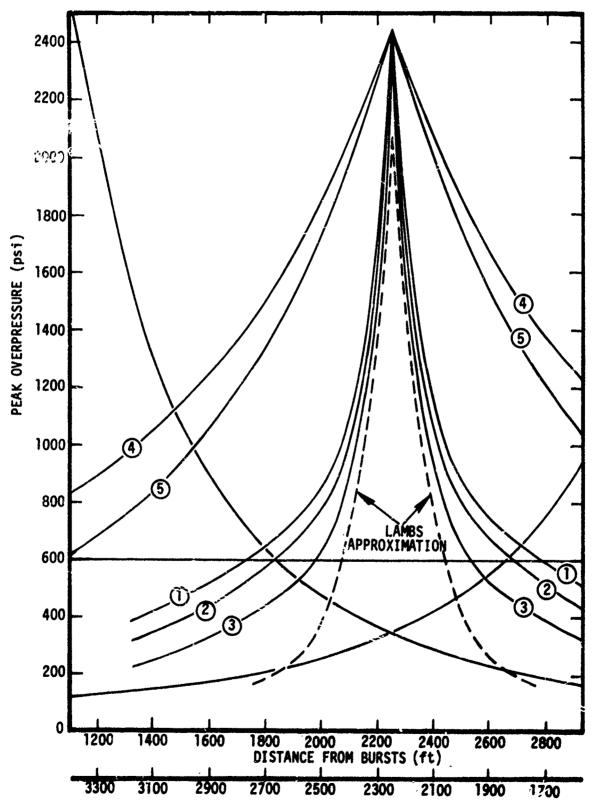


Figure 5. Approximations for the Peak Overpressure between Two Simultaneous 1 MT Surface Bursts 4500 ft Apart

bursts (1-MT) separated by 4500 ft. Table 2 illustrates the development of numerical values for each case.

- (1) The peak interaction is defined as the local pressure in front of the transmitted blast wave multiplied by the initial reflection factor for the colliding shock fronts (reflection factor RF \simeq 7.0).
- (2) The peak interaction pressure is defined as the local pressure in front of the transmitted blast wave multiplied by the reflection factor appropriate for a shock of strength equal to that of the second shock if it had expanded (unreflected) to that distance beyond the initial contact point.
- (3) The peak interaction pressure is defined as the local pressure in front of the transmitted blast wave multiplied by the reflection factor for a shock of peak pressure equal to that pressure.
- (4) The peak interaction pressure is defined as the unreflected (incident) shock pressure multiplied by the reflection factor appropriate to the time of first contact (RF = 7.0).
- (5) The peak interaction pressure is defined as the unreflected (incident) shock pressure multiplied by the reflection factor appropriate for that reduced shock strength as it expands in an undisturbed sea level atmosphere.

1-MT Simultaneous Burst Interaction (Separated by 4500 ft) Approximations to Peak Overpressure Table 2.

⊕ ~£	Ø 7.£	Φ ^{ΔP} S (psi)	. R	(Eqn 3)	Φ ^P _i (psi)	CASE 1 OPR (psi) 7.0 × ©	CASE 2 OP R (ps i)	CASE 3 © AP AP (pst) Ø×©	CASE 4 APR (psi) 7.0 x ③	CASE 5 APR (psi) 3×4
2250	2250	350	7.0	7	350	2450	2450	2450	2450	2450
2120	2380	300	6.8	5.9	170	1190	1160	1000	2100	2040
1990	2510	260	9.9	5.2	120	840	790	620	1820	1720
1870	2630	230	6.4	4.9	100	700	640	490	1610	1470
1730		500	6.2	4.6	8	260	200	370	1400	1240
1610	2890	180	6.0	4.4	20	490	420	300	1260	· 1080
1530	2970	168	5.8	4.2	65	455	380	270	1180	970
1420	3080	152	5.66	4.0	57	400	320	230	1060	610

None of these approximations account for the expansion of both shocks as they pass through each other. The most reasonable approximations are (3) and (2), but the others are shown for comparison (Figure 5).

The extra line target coverage for this example (1-MT bursts separated by 4500 ft) is listed in Table 3.

Table 3. Comparison of Range and Area Coverage Increases for Five Different Approximations to the Interaction of Two Simultaneous 1-MT Surface Bursts Separated by 4500 ft

APPROXIMATION NUMBER	PEAK OVERPRESSURE COVERED (psi)	SINGLE BURST RANGE (ft)	DISTANCE ADDED BY INTERACTION (ft)	RANGE INCREASE (%)
3ª	540	1915	670	17
2 ^a	610	1830	840	23
1	640	1800	910	25
5	990	1540	1410	46
4	1120	1470	1550	53

amost plausible approximations.

The last two are clearly overestimates of the effect, but the first three may also predict more enhancement than is real.

Further estimates are given in the following sections.

SECTION 3. INTERACTION OF UNEQUAL SHOCKS

The preceding discussion has dealt with the case of two simultaneous bursts (equal strength shocks) interacting. Interactions between shocks of unequal strength are also of interest, since timing of multiple bursts may not be exact and the first blast may be considerably weaker by the time the second blast meets it.

Suppose two shocks meet when their respective peak overpressures are ΔP_1 and ΔP_2 , and suppose the first is stronger than the second $(\Delta P_1 > \Delta P_2)$. These shocks, on interacting, lead to an overpressure ΔP_R , a density $\rho_R^{\quad *}$ and a resultant particle velocity U_R . Figure 6 identifies the nomenclature in which two initial shocks have met and have resulted in two transmitted shocks which have velocities U_{R1} and U_{R2} directed away from each other, and a particle velocity U_R which is positive to the right if $\Delta P_1 > \Delta P_2$.

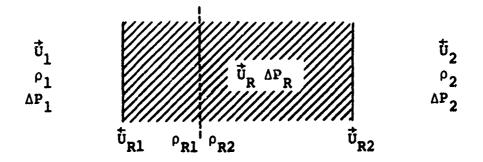


Figure 6. Shock Interaction Notation for Unequal Shocks

Actually, two states of density and temperature separated by a contact discontinuity exist in the shock interaction region (shaded area, Figure 6), but pressure and velocity are the same in both states, viz., $\Delta P_{\rm R}$, $H_{\rm R}$.

From standard shock relations, \vec{U}_1 , \vec{U}_2 , μ_1 , and μ_2 are expressible in terms of ΔP_1 and ΔP_2 and are considered as known here.

$$U_{1} = \Delta P_{1} \left(\frac{(\gamma+1)}{2} \Delta P_{1} + \gamma P_{0} \right)^{-1/2} \sqrt{\rho_{0}}$$

$$U_{2} = \Delta P_{2} \left(\frac{(\gamma+1)}{2} \Delta P_{2} + \gamma P_{0} \right)^{-1/2} \sqrt{\rho_{0}}$$

$$\rho_{1} = \rho_{0} \left[\left(\frac{(\gamma+1)}{2} \right) \Delta P_{1} + \gamma P_{0} \right] \left[\left(\frac{(\gamma-1)}{2} \right) \Delta P_{1} + \gamma P_{0} \right]^{-1}$$

$$\rho_{2} = \rho_{0} \left[\left(\frac{(\gamma+1)}{2} \right) \Delta P_{2} + \gamma P_{0} \right] \left[\left(\frac{(\gamma-1)}{2} \right) \Delta P_{2} + \gamma P_{0} \right]^{-1} . \quad (6)$$

Expressing the conservation of mass flow rate through each shock, one may write

$$\rho_{R1}(U_{R1} + U_{R}) = \rho_{1}(U_{1} + U_{R1}) ,$$

$$\rho_{R2}(U_{R2} - U_{R}) = \rho_{2}(U_{2} + U_{R2}) .$$
(7)

The momentum change related to the pressure jumps at the shocks can be expressed as

$$\Delta P_{R} - \Delta P_{1} = \rho_{1} U_{1} (U_{1} + U_{R1}) - \rho_{R1} U_{R} (U_{R} + U_{R1})$$

$$\Delta P_{R} - \Delta P_{2} = \rho_{2} U_{2} (U_{2} + U_{R2}) + \rho_{R2} U_{R} (U_{R2} - U_{R}) . \qquad (8)$$

Eliminating $\mathbf{U}_{\mathbf{R}\mathbf{1}}$ and $\mathbf{U}_{\mathbf{R}\mathbf{2}}$ from Equations 6 and 7, one can write

$$\Delta P_{R} = \Delta P_{1} + \frac{\rho_{1}^{\rho} R_{1}}{\rho_{R_{1}} - \rho_{1}} (U_{1} - U_{R})^{2}$$

and

$$\Delta P_{R} = \Delta P_{2} + \frac{\rho_{2} \rho_{R2}}{\rho_{R2} - \rho_{2}} (U_{2} + U_{R})^{2} . \qquad (9)$$

The initial energy density (E) jump conditions at each transmitted shock require

$$E_R - E_1 = \frac{P_R + P_1}{2} \left(\frac{1}{\rho_1} - \frac{1}{\rho_{R1}} \right)$$

and

$$E_R - E_2 = \frac{P_R + P_2}{2} \left(\frac{1}{\rho_2} - \frac{1}{\rho_{R2}} \right)$$
 (10)

If one assumes an ideal gas with ratio of specific heats (γ), then E = P/[(γ -1) ρ]. Solving for ρ_R leads to

$$\frac{\rho_{R1}}{\rho_1} = \frac{(\gamma+1)\Delta P_R + (\gamma-1)\Delta P_1 + 2\gamma P_0}{(\gamma-1)\Delta P_R + (\gamma+1)\Delta P_1 + 2\gamma P_0}$$

and

$$\frac{\rho_{R2}}{\rho_2} = \frac{(\gamma+1)\Delta P_R + (\gamma-1)\Delta P_2 + 2\gamma P_0}{(\gamma-1)\Delta P_R + (\gamma+1)\Delta P_2 + 2\gamma P_0} . \tag{11}$$

Using Equations 10 and the Hugoniot relations to express ρ_1 , ρ_2 , U_1 , and U_2 in terms of ΔP_1 and ΔP_2 (Equation 6), one can derive

$$\Delta P_{R} = A \pm \sqrt{A^2 + C} \tag{12}$$

and

$$\Delta P_{R} = D \pm \sqrt{D^{2} + F}$$
 (13)

in which

$$A = \Delta P_{1} + \frac{\gamma+1}{4} \rho_{1} (U_{1} - U_{R})^{2}$$

$$C = -\Delta P_{1}^{2} + \left(\frac{\gamma-1}{2} \Delta P_{1} + \gamma P_{0}\right) \rho_{1} (U_{1} - U_{R})^{2}$$

$$D = \Delta P_{2} + \frac{\gamma+1}{4} \rho_{2} (U_{2} + U_{R})^{2}$$

$$F = -\Delta P_{2}^{2} + \left(\frac{\gamma-1}{2} \Delta P_{2} + \gamma P_{0}\right) \rho_{2} (U_{2} + U_{R})^{2}$$

These equations can be solved for ΔP_R by iterative selection of the velocity U_R (all other values being predetermined by the values of γP_0 , ΔP_1 , and ΔP_2).

A set of example values of the resultant peak overpressure $\Delta P_{\rm R}$ for two shocks meeting when one of them is 100 psi is illustrated in Figure 7 for two values of the specific heat ratio. For example, a 100-psi and a 500-psi shock meet to give more than 1500 psi for γ = 1.4 and about 2000 psi for γ = 1.2.

Figure 8 illustrates the peak pressure amplification from the meeting of two shocks with a plot of the ratio of the resulting peak overpressure to the sum of the two incident peak pressures. The amplification approaches unity if one of

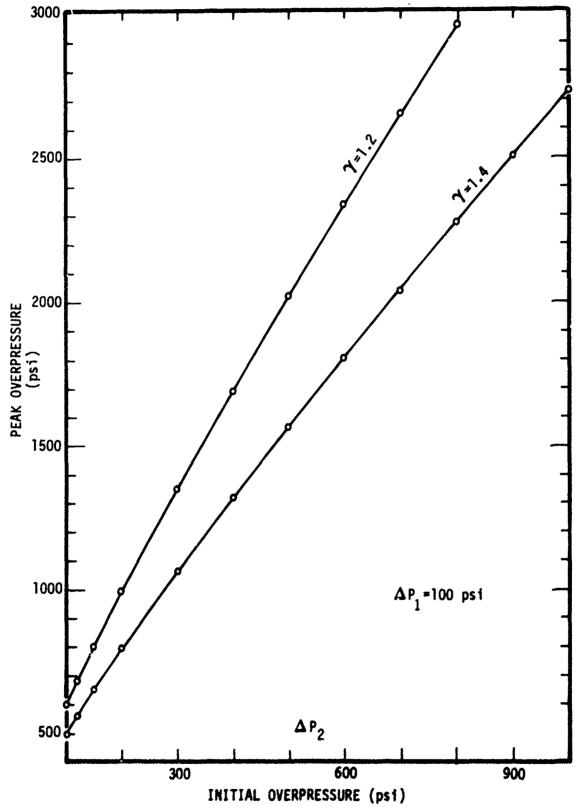
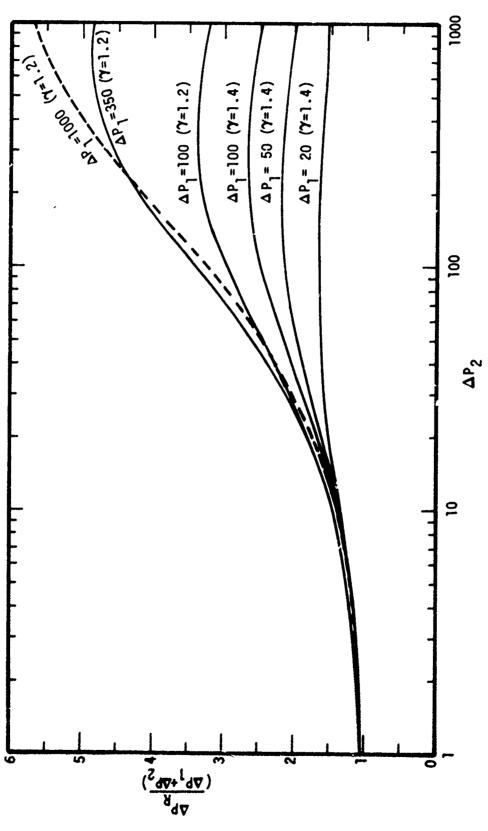


Figure 7. Resultant Peak Overpressure from Two Shocks (One at 100 psi)



the shocks is weak, and seems to reach a peak when the ratio of the two incident overpressures lies between 3 and 5.

This solution for the resultant peak pressure from the collision of two unequal shocks suggests yet another approximation to the peak overpressure distribution for our example of two simultaneous 1-MT bursts separated by 4500 ft (Figure 5). The interior overpressure (behind the shock front) that a transmitted shock encounters can be assumed to act similarly to a shock of that overpressure, and the resultant overpressure computed (by means of Equations 12 and 13). This approximation is tabulated in Table 4 and illustrated in Figure 9 (labeled Case 6).

This approximation, using unequal shock properties, is not very different from the simple average of the peak overpressures from the earlier bounding cases—Cases 3 and 5—which use the interior blast wave pressure multiplied by the normal shock reflection factor for that pressure (Case 3) and the single shock peak overpressure multiplied by its normal reflection factor (Case 5). This average is also shown in Figure 9 as Case 7.

Table 4. 1-MT Simultaneous Burst Interaction Peak Overpressure Approximations Using Unequal Shock Results

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CASE 7 APR (psi) 9 + 11 (TABLE 1)	2460	1515	1170	975	795	685	630	545
ΔP _R (ΔP _S +ΔP _i) psi	7.0	3.1	2.8	2.67	2.51	2.41	2.36	2.75
CASE 6 APR (psi)	2460	1450	1070	880	700	009	550	475
⊘ ≻	1.355	1.37	1.39	1.395	1.397	1.399	1.40	1.40
$\begin{array}{c} \textcircled{0} \\ \Delta^{p}_{i} \\ (psi) \\ \Delta^{p}(r_{2}) \end{array}$	350	170	120	100	8	20	65	57
ΔPS (psi)	350	300	260	230	500	180	168	152
0- 1	2250	2380	2510	2630	2770	2890	2970	3080
Θ ⁷ 2ξ	2250	2120	1990	1870	1730	1610	1530	1420

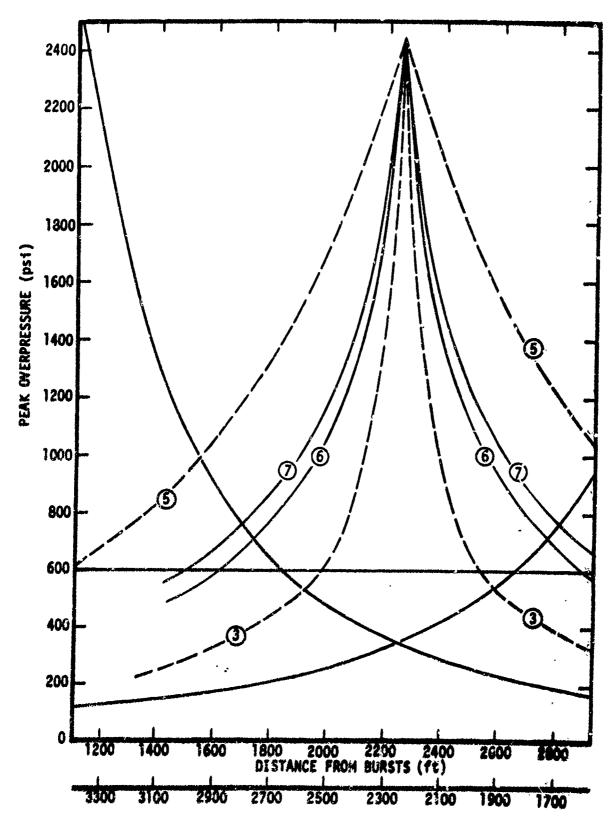


Figure 9. Further Approximations for the Peak Overpressure between Two Simultaneous 1 MT Surface Bursts 4500 ft Apart

SECTION 4. COMPARISON WITH THE LAMB PROCEDURE

A more careful accounting for the usual conservation of mass, momentum, and energy during these shock interactions requires some further assumptions and more geometry and arithmetic. Such an attempt is the basis of extensive calculations and predictions at the Air Force Weapons Laboratory with a program referred to as LAMB [6].

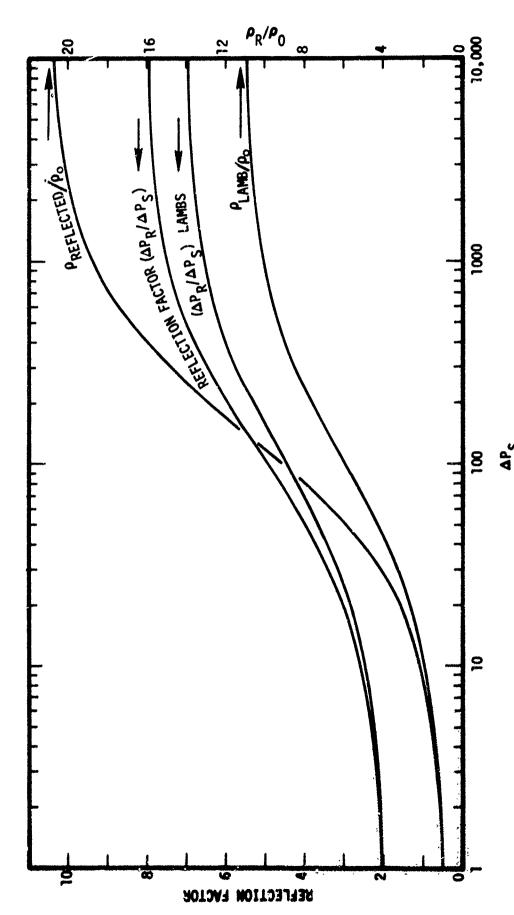
The essential features of this procedure are as follows: Mass conservation; assume:

$$\rho = \rho_0 + \sum_{i=1}^{n} \Delta \rho_i, \quad (\rho \ge 0.5 \ \rho_0)$$
 (14)

in which ρ is the air density, ρ_0 the ambient (pre-shock) air density, and $\Delta \rho_1$ is the over-density ($\rho_1 - \rho_0$) in each blast wave.

Recognize that densities in strong shock fronts may rise to more than ten times the ambient density, but may also fall to less than one-tenth the ambient value inside the fireball. This prescription predicts the peak density of two equal colliding strong shocks to be only about half of the correct Hugoniot value. (See Figure 10.)

The program, originally designed to approximate overlapping bursts at altitudes between 10 and 30 kft (in a missile defense role), quite arbitrarily restricts the underdensities (negative overdensities) to half (or more) of the ambient density. Such a restriction provides a reasonable, if unsatisfactorily empirical accounting of other dispersive



 ΔP_S Figure 10. Comparison of Reflection Factor (Δ^0_R/Δ^0_S) for Normal Shocks and by the Lambs Hethod; Comparison of Reflected Density and Density by Lambs Method

effects likely to occur in the high temperature (low density) interior of a nuclear fireball, but it cannot be justified rigorously (from first principles). Actually, some such limit is needed to prevent an undesired increase in net kinetic energy for a shock in the very low density interior of a strong blast wave (fireball) that would result otherwise from this prescription. Recognize also that this expression is not one of mass conservation, but prescribes density, or mass-per-unit volume. It has long been a favorite piece of magic for simplified blast solutions (many published as serious contributions) to make seemingly innocuous assumptions about density distributions and then proceed to unfold a marvelously consistent picture of some blast wave. The rabbit is always already in the hat here, however, since density distributions are, in fact, integral representations of the entire movement history of the blast, and the movements so described are a direct consequence of the acceleration or force (pressure gradient) history. So any density profile contains the blast wave history to that instant, and is not a trivially adjustable parameter of small consequence.

Conservation of momentum; assume:

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$$\rho \vec{\mathbf{v}} = \sum_{i=1}^{n} \rho_{i} \vec{\mathbf{v}}_{i}$$
 (15)

where ρ_i is the density in the i^{th} blast wave, $\vec{\nu}_i$ is the particle velocity of the i^{th} blast wave, and ρ and $\vec{\nu}$ are the resultant density and particle velocity in the blast interactions. This represents a local momentum density vector sum without consideration of pressure impulse contributions, which is not quite consistent with the usual assumptions of inviscid gas dynamics for blast wave characterization.

Conservation of energy; assume:

$$\Delta P = P - P_0 = \sum_{i=1}^{n} \Delta P_i + \frac{1}{2} \left[\sum_{i=1}^{n} \rho_i v_i^2 - \rho v^2 \right]$$
 (16)

in which $\Delta P_i = P_i - P_0$ is the overpressure in the ith blast, and ΔP is the resulting overpressure in the interacting blasts.

This prescription purports to convert excess kinetic energy from the opposing flows into pressure energy, a procedure consistent with normal hydrodynamic flow characterizations. However, it is inexact as an energy equivalent to add $1/2~\rho v^2$ terms to overpressure. The dimensions are correct, but the compressibility factor $1/(\gamma-1)$ is missing. As a consequence, the reflection factor for two equal shocks resulting from this prescription is slightly in error. For an ideal gas:

$$\left(\frac{\Delta P_{r}}{\Delta P}\right)_{LAMB} = R_{LAMB} = \frac{2\gamma \Delta P + 4\gamma P_{o}}{(\gamma - 1)\Delta P + 2\gamma P_{o}} . \qquad (17)$$

More rigorously (as in Equation 3),

$$\frac{\Delta P_{r}}{\Delta P} = R = \frac{(3\gamma - 1)\Delta P + 4\gamma P_{o}}{(\gamma - 1)\Delta P + 2\gamma P_{o}} \qquad (18)$$

These two formulae are compared in Figure 10 for $1 < \Delta P < 10^4$, showing the LAMB procedure to be low by a factor of 7/8 at high overpressures ($\gamma = 1.4$).

The LAMB procedure, when applied to the previous example (two simultaneous 1-MT surface bursts 4500 ft apart), gives even less coverage with high pressure than the previous

estimates using peak reflection factors. As mentioned, the LAMB method misses the peak pressure by a factor approaching 7/8, and drops away from that peak value very rapidly (Figure 11). Table 5 compares the range enhancements from the approximations previously discussed with that for the LAMB model. The curves in Figure 11 and the basic data in Tables 2 and 4 are derived from Reference 1, but any of the descriptions in References 3, 4 or 5 would serve as well.

The added line coverage for this example with the LAMB procedure is about 11 percent, a smaller effect than any of the approximations given in the previous section. Good agreement with experiments is claimed for the LAMB model when applied to HE tests or to the shock reflections on a nuclear test such as PLUMBBOB-PRISCILLA. However, the arbitrary assumptions in the model are neither intuitive nor physically correct, and their effect on results far from the point of initial shock contact remains unclear.

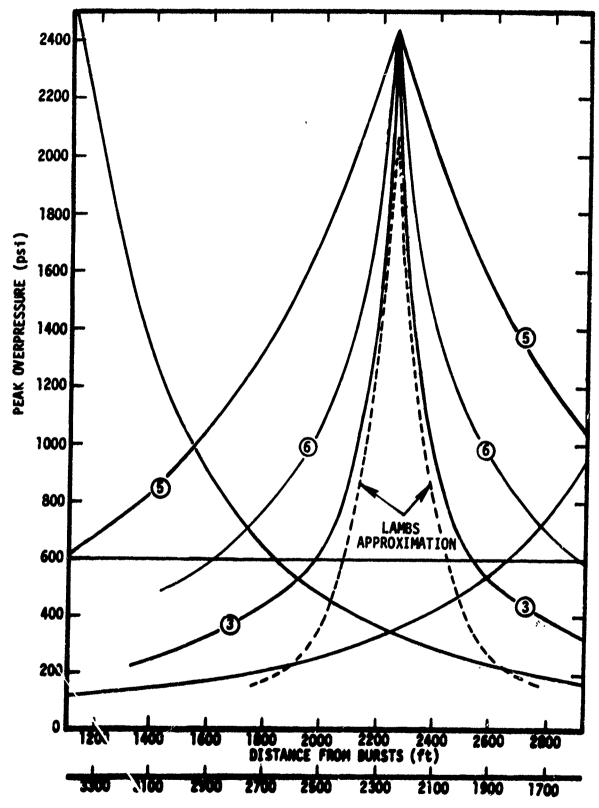


Figure 11. Approximations for the Peak Overpressure between Two Simultaneous 1 NT Surface Bursts 4500 ft Apart Compared with the LAMB Model

Table 5. Range Coverage Comparisons (1-MT Bursts 4500 ft Apart)

APPROXIMATION CASE NUMBER	PEAK OVERPRESSURE COVERED (psi)	SINGLE BURST RANGE (ft)	DISTANCE ADDED BY INTERACTION (ft)	PERCENT RANGE INCREASE (%)
LAMB	450	2030	430	11
3	540	1915	670	17
6	710	1730	1040	30
5	990	1540	1410	35

SECTION 5. SUMMARY AND CONCLUSIONS

A reasonable lower limit approximation to the combined overpressure would appear to be to multiply the pressure at a point inside a single blast and in front of the transmitted shock from a second burst by the reflection factor for a shock of that interior pressure (Case 3). A similarly simple upper bound should be provided by multiplying the single blast peak overpressure by the normal reflection factor for that pressure at distances beyond the point of first contact for the two shocks (Case 5). A further procedure, almost as simple, providing an intermediate value, uses the pressure predicted for the interaction of unequal shocks, based on the pressure ahead of and behind the transmitted shock (Case 6).

The LAMB procedure is not rigorously correct, but it provides a more general and a more detailed treatment of interacting shocks. Unfortunately, it is not clear whether it overestimates or underestimates the resulting pressures, although all the predictions for this example lie above the LAMB-derived values. Accepting all the apparent uncertainty in these approximations to multiple shock interactions, one can still conclude that:

- The region of enhanced overpressures from two simultaneous separate blast waves is a small fraction of the area covered by each individual blast.
- The extra coverage of a line target with high overpressures (ΔP_S > 300 psi) is of the order of 10-50 percent, and, more probably, less than 30 percent.

• The LAMB procedure may, in some cases, underpredict the peak pressures for interacting blast waves.

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